

# 3

91577



NEW ZEALAND QUALIFICATIONS AUTHORITY  
MANA TOHU MĀTAURANGA O AOTEAROA

QUALIFY FOR THE FUTURE WORLD  
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SUPERVISOR'S USE ONLY

## Level 3 Calculus, 2018

### 91577 Apply the algebra of complex numbers in solving problems

9.30 a.m. Tuesday 13 November 2018  
Credits: Five

Achievement	Achievement with Merit	Achievement with Excellence
Apply the algebra of complex numbers in solving problems.	Apply the algebra of complex numbers, using relational thinking, in solving problems.	Apply the algebra of complex numbers, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

**You should attempt ALL the questions in this booklet.**

Show ALL working.

Make sure that you have the Formulae and Tables Booklet L3–CALCF.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

Check that this booklet has pages 2–12 in the correct order and that none of these pages is blank.

**YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.**

**TOTAL**

ASSESSOR'S USE ONLY

**QUESTION ONE**ASSESSOR'S  
USE ONLY

- (a) What is the remainder when  $2x^3 - 3x^2 + 4x + 3$  is divided by  $x - 2$ ?

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- (b) If  $u = m \operatorname{cis} \frac{\pi}{3}$  and  $v = m^3 \operatorname{cis} \frac{2\pi}{5}$ , find  $uv$  in polar form.

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- (c) Solve the equation  $2 + \sqrt{x} = \sqrt{x+k}$  for  $x$  in terms of  $k$ .

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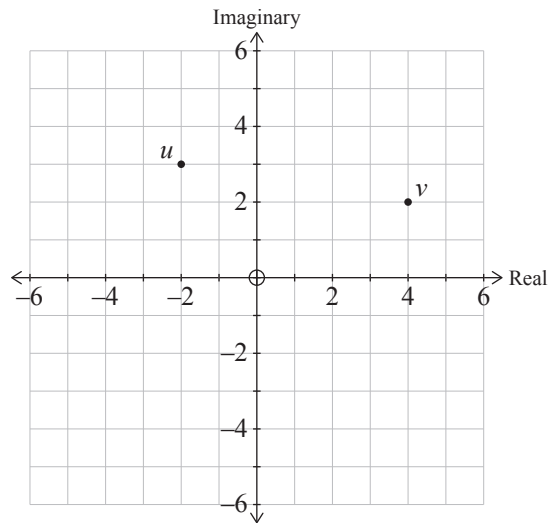




**QUESTION TWO**

- (a) Complex numbers  $u$  and  $v$  are represented on the Argand diagram below.

If  $w = u + \bar{v}$ , show  $w$  on the Argand diagram.



- (b) Write  $\frac{6}{3-\sqrt{7}}$  in the form  $a + b\sqrt{7}$ .

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- (c) One solution of the equation  $z^3 + Az^2 + 34z - 40 = 0$  is  $z = 3 + i$ .

If  $A$  is a real number, find the value of  $A$  and the other two solutions of the equation.

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- (d) If  $z = \frac{15}{1-2i} - 2i$ , find  $\text{mod}(z)$ .

*You must show all algebraic working.*

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